

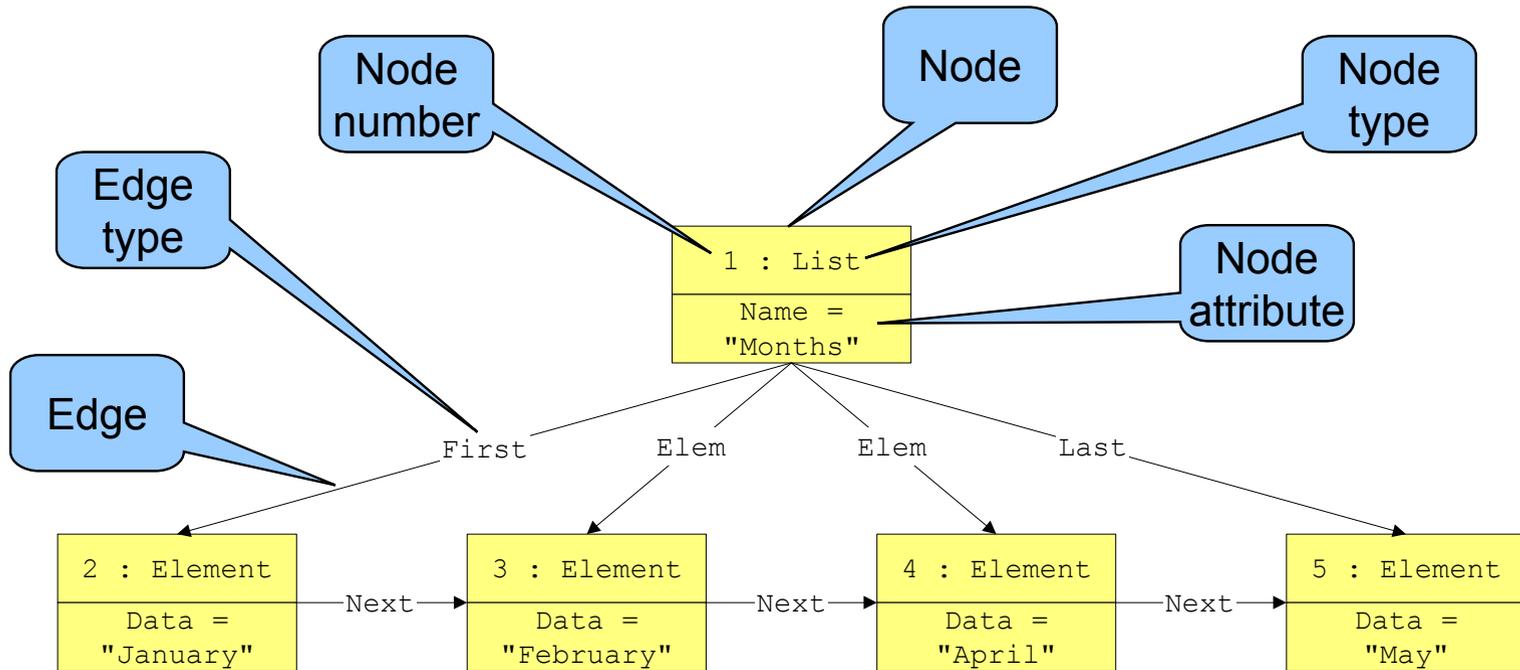
# Specification with Graph Rewriting Systems

## Characterization

- ❑ Formal specification of abstract data types
- ❑ Model-oriented specification
- ❑ Graphs as underlying data model
- ❑ Specification of read operations by graph tests, specification of write operations by graph rewrite rules
- ❑ Proof technique: induction
- ❑ Rapid Prototyping by generating code from the specification

## Introductory Example

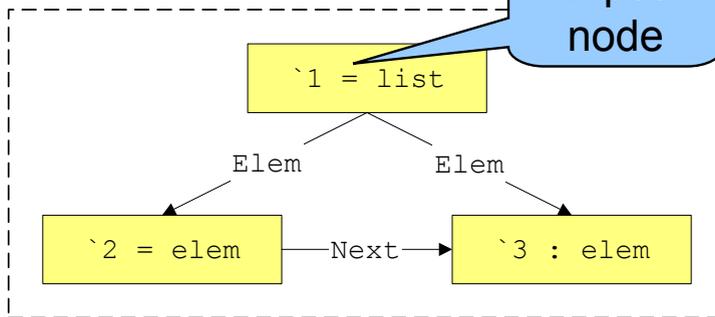
## Representation of a list as a graph



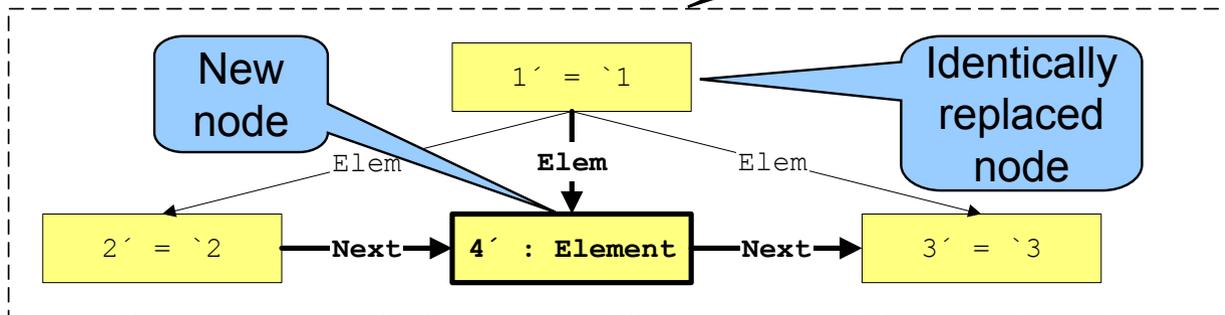
## Example of a graph rewrite rule

production PostInsertElement

(list : List; elem : Element; data : string;  
out new : Element) =



::=



attribute transfer 4'.Data := data;

return new := 4';

end;

Name

Parameter

Left-hand side

Right-hand side

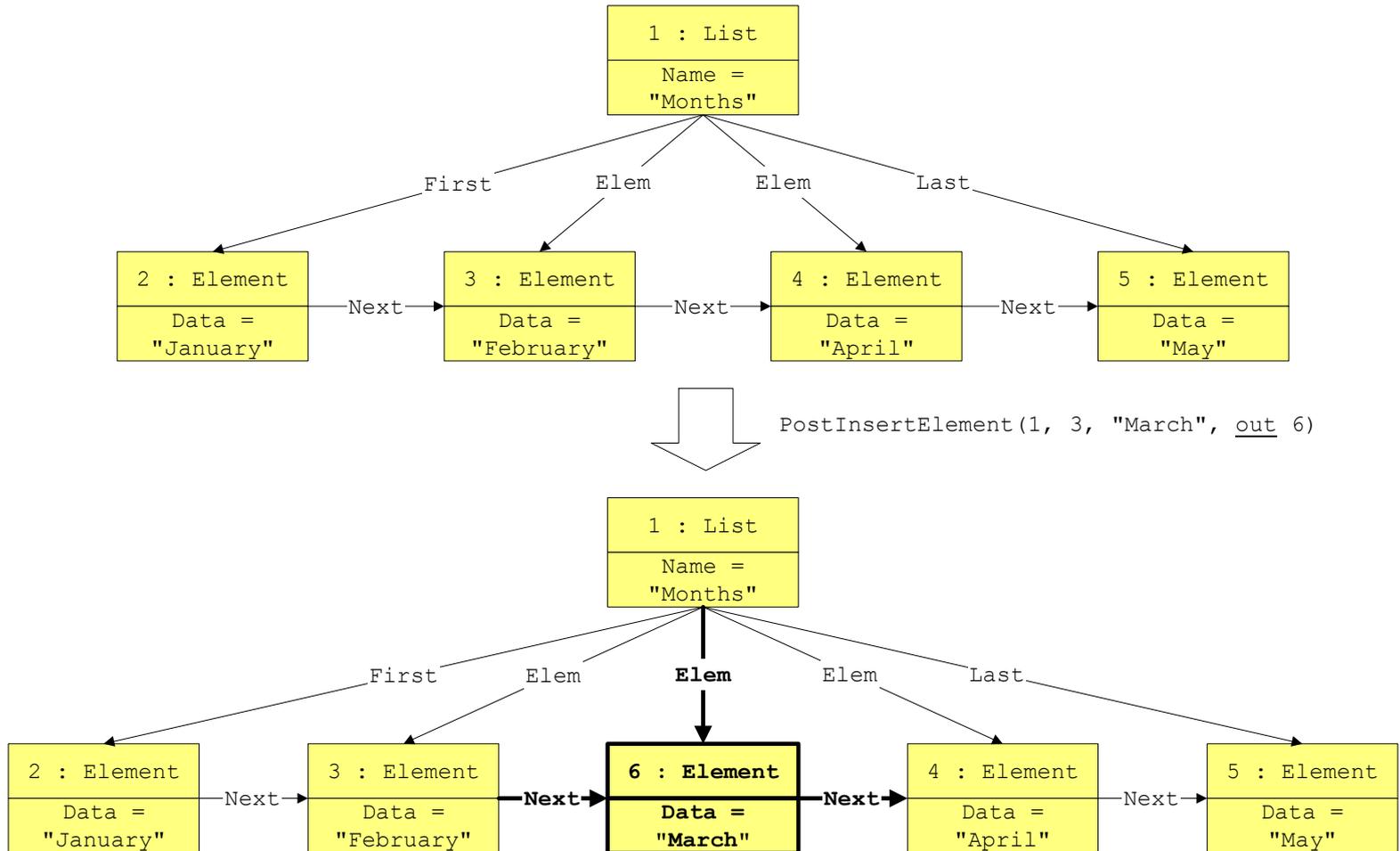
New node

Identically replaced node

Attribute assignments

Return part

## Application of the graph rewrite rule



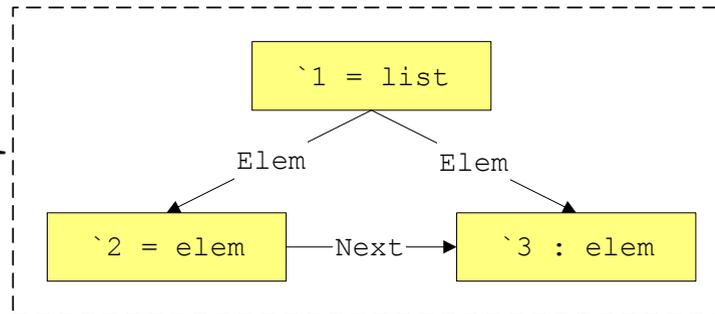
## Example of a graph test

Name

Parameter

```
test GetNextElement  
  (list : List; elem : Element; out next : Element) =
```

Graph



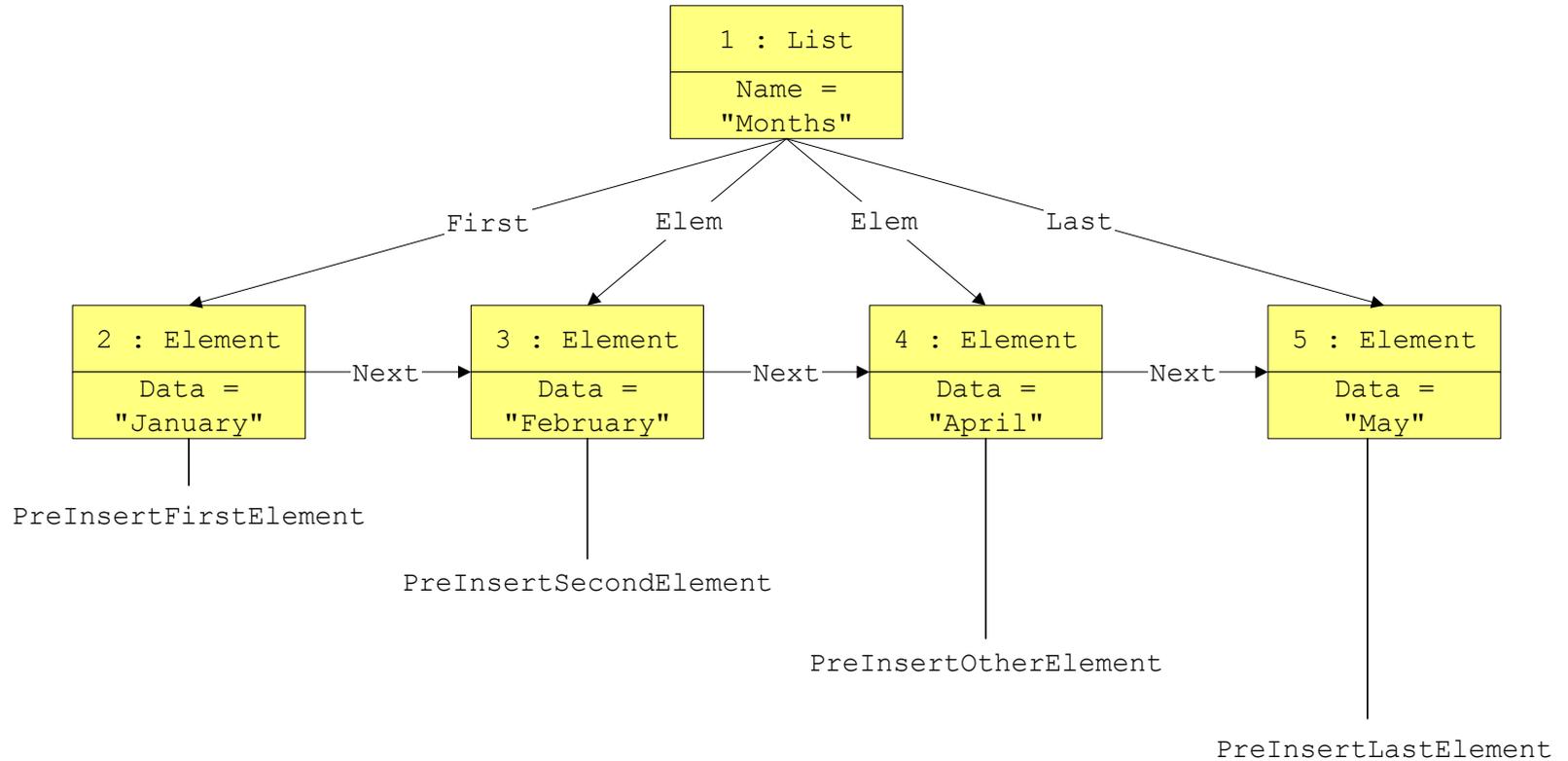
```
return next := `3;  
end;
```

Return  
part

## Interface of the abstract data type List

<b>List creation and deletion</b>	
CreateList	Creation of a list
DeleteList	Deletion of a list
<b>Write operations</b>	
InsertFirstElement	Insertion into an empty list
PreInsertElement	Insertion before an element
PostInsertElement	Insertion after an element
DeleteElement	Deletion of an element
<b>Read operations</b>	
IsEmpty	List empty?
GetFirstElement	First element
GetLastElement	Last element
GetNextElement	Next element
GetPreviousElement	Previous element
GetData	Data of current element

# Cases of PreInsertElement



## Example of programming with graph rewrite rules

Transaction

Name

Parameter

```
transaction PreInsertElement  
  (list : List; elem : Element; data : string;  
   out new : Element) =  
  choose  
    PreInsertFirstElement(list, elem, data, out new)  
  or  
    PreInsertSecondElement(list, elem, data, out new)  
  or  
    PreInsertOtherElement(list, elem, data, out new)  
  or  
    PreInsertLastElement(list, elem, data, out new)  
  end  
end;
```

Control  
structure

# Theoretical Foundations

## Graphs

### Definition: Directed, labeled graph

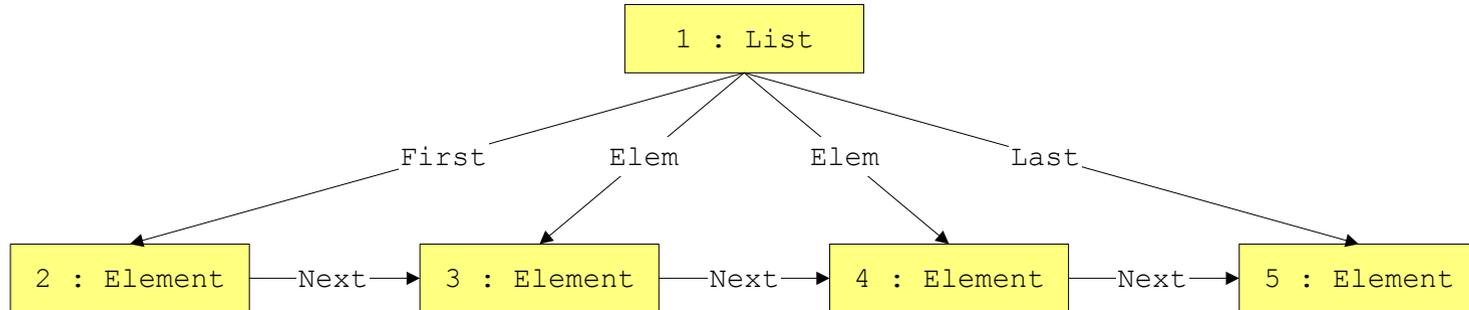
$G = (V, E, I)$  is a directed graph over label sets  $L_V$  (labels for vertices) and  $L_E$  (labels for edges)  $\Leftrightarrow$

- »  $V$  is a set of nodes (node identifiers).
- »  $E \subseteq V \times L_E \times V$  is a set of labeled edges.
- »  $I: V \rightarrow L_V$  is a labeling function for nodes.

### Remarks:

- ❑ Nodes have identifiers, but not edges.
- ❑ Thus, there are no parallel edges with the same labels.
- ❑ Edges are binary relationships.
- ❑ Nodes and edges are typed (labeled).
- ❑ So far, neither nodes nor edges are attributed.

## Example of a directed graph



$G = (V, E, I)$  with:

- $V = \{1, 2, 3, 4, 5\}$
- $E = \{(1, \text{First}, 2), (1, \text{Elem}, 3), (1, \text{Elem}, 4), (1, \text{Last}, 5), (2, \text{Next}, 3), (3, \text{Next}, 4), (4, \text{Next}, 5)\}$
- $I = \{(1, \text{List}), (2, \text{Element}), (3, \text{Element}), (4, \text{Element}), (5, \text{Element})\}$

## Partial graphs and subgraphs

### Definition: Partial graph

$G = (V, E, l)$  is a partial graph of  $G' = (V', E', l')$   $\Leftrightarrow$

- »  $V \subseteq V'$ , i.e., the nodes of  $G$  are also contained in  $G'$ .
- »  $E \subseteq E'$ , i.e., the edges of  $G$  are contained in  $G'$ .
- »  $l' \upharpoonright_V = l$ , i.e., the nodes of  $G$  have the same labels in  $G'$ .

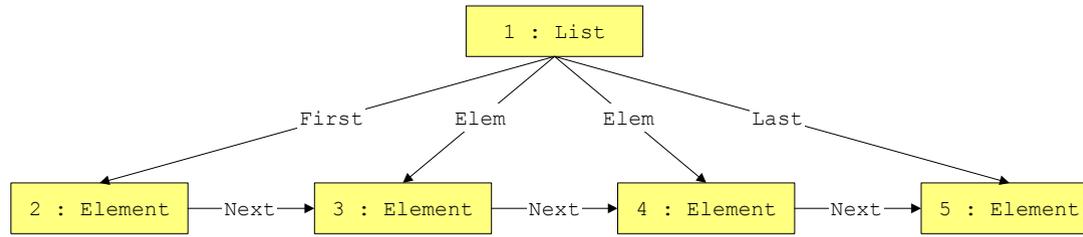
### Definition: Subgraph

$G = (V, E, l)$  is a subgraph of  $G' = (V', E', l')$   $\Leftrightarrow$

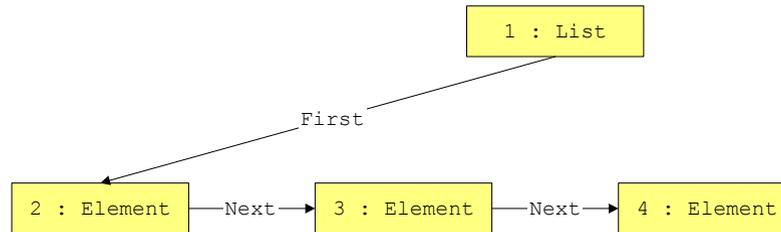
- »  $G$  is a partial graph of  $G'$ .
- »  $E = \{ (v_1, e, v_2) \in E' \mid v_1, v_2 \in V \}$   
 $G$  contains all edges of  $G'$  whose sources and targets are common to  $G$  and  $G'$ .

## Example of partial graphs and subgraphs

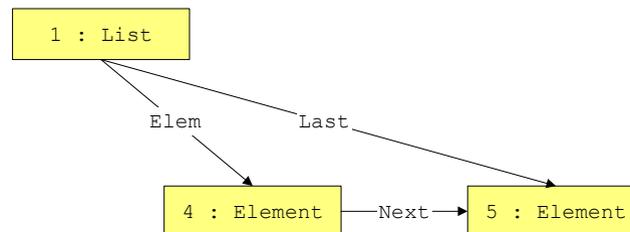
### Graph



### Partial graph



### Subgraph



## Graph morphisms

### Definition: Graph morphism

A function  $h : V \rightarrow V'$  is a graph morphism from  $G$  to  $G'$ , i.e.,  
 $h : G \rightarrow G' \Leftrightarrow$

- »  $\forall v \in V : l'(h(v)) = l(v)$ , i.e., labels are preserved.
- »  $\forall (v_1, el, v_2) \in E : (h(v_1), el, h(v_2)) \in E'$ , i.e., edges are preserved.

### Definition: Graph isomorphism

A graph morphism  $h : G \rightarrow G'$  is a graph isomorphism  $\Leftrightarrow$

- »  $h : V \rightarrow V'$  is injective and surjective
- »  $h : V \rightarrow V'$  induces a function  $h' : E \rightarrow E'$ , which must be injective and surjective, as well.

## Set-theoretic graph operations (1)

### Definition: Union of graphs

Let  $G$  and  $G'$  be directed graphs,  $I \mid_{V \cap V'} = I' \mid_{V \cap V'}$ :

»  $G \cup G' = G'' = (V'', E'', I'')$  with

$$\Rightarrow V'' = V \cup V'$$

$$\Rightarrow \forall v \in V'' : I''(v) = \text{if } v \in V \text{ then } I(v) \text{ else } I'(v) \text{ end}$$

$$\Rightarrow E'' = E \cup E'$$

»  $G \oplus G'$  disjoint union of  $G$  and  $G'$ :

Rename nodes of  $G$  or  $G'$  such that  $V \cap V' = \emptyset$ ,  
and apply the graph union defined above:

$$G \oplus G' = G \cup G'.$$

## Set-theoretic graph operations (2)

### Definition: Difference of graphs

Let  $G$  and  $G'$  be directed graphs,  $I \upharpoonright_{V \cap V'} = I' \upharpoonright_{V \cap V'}$ :

»  $G \setminus G' = G'' = (V'', E'', I'')$  with

$$\Rightarrow V'' = V \setminus V'$$

$$\Rightarrow I'' = I \upharpoonright_{V''}$$

$$\Rightarrow E'' = E \setminus E' \text{ (without deletion of dangling edges)}$$

»  $G \setminus\setminus G' = G'' = (V'', E'', I'')$  with

$$\Rightarrow V'' = V \setminus V'$$

$$\Rightarrow I'' = I \upharpoonright_{V''}$$

$$\Rightarrow E'' = (E \setminus E') \cap (V'' \times L_E \times V'') = E \cap (V'' \times L_E \times V'')$$

(with deletion of dangling edges)

## Set-theoretic graph operations (3)

### Definition: Intersection of graphs

Let  $G$  and  $G'$  be directed graphs,  $I \upharpoonright_{V \cap V'} = I' \upharpoonright_{V \cap V'}$ :

»  $G \cap G' = G'' = (V'', E'', I'')$  with

$$\Rightarrow V'' = V \cap V'$$

$$\Rightarrow I'' = I \upharpoonright_{V''}$$

$$\Rightarrow E'' = E \cap E'$$

## Graph rewrite rules

### Definition: Graph rewrite rule

A graph rewrite rule is a triple  $r = (L, K, R)$  with:

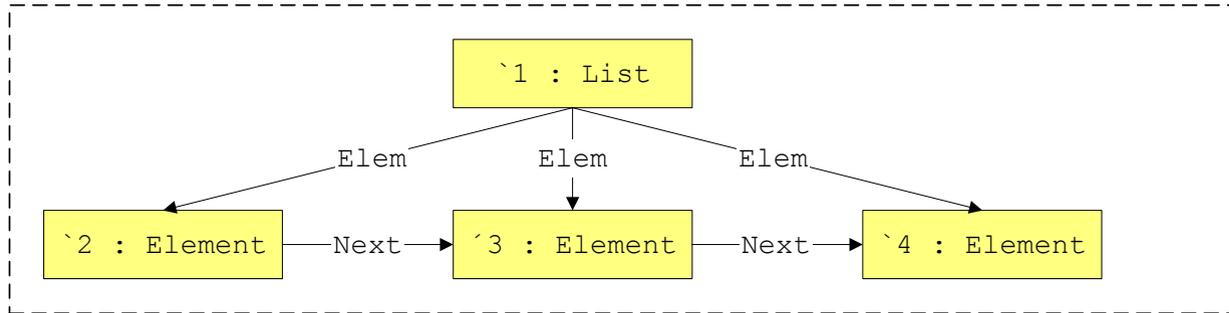
- »  $L$ , the left-hand side of  $r$ , is a graph.
- »  $R$ , the right-hand side of  $r$ , is a graph.
- »  $K = L \cap R$  is the gluing graph.

### Remarks

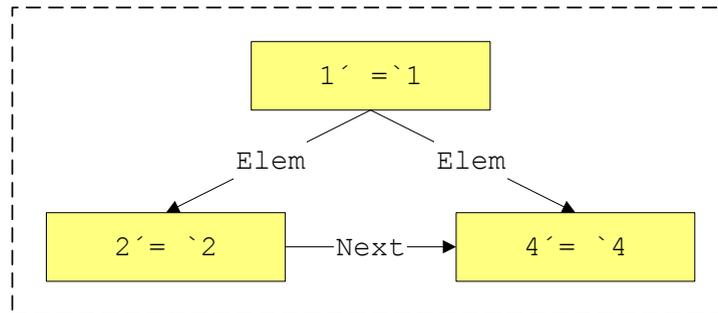
- ❑ Elements of  $L$  but not of  $K$  are deleted.
- ❑ Elements of  $R$  but not of  $K$  are inserted.
- ❑ Elements of  $K$  are preserved.
- ❑  $K$  is called gluing graph because it is used for the embedding of new nodes of  $R$ .

## Example of a graph rewrite rule (1)

production DeleteElement =



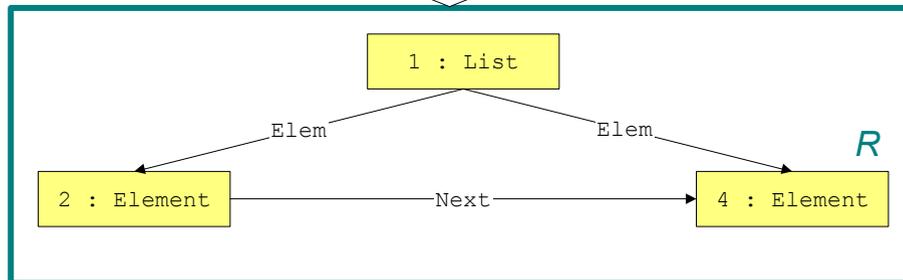
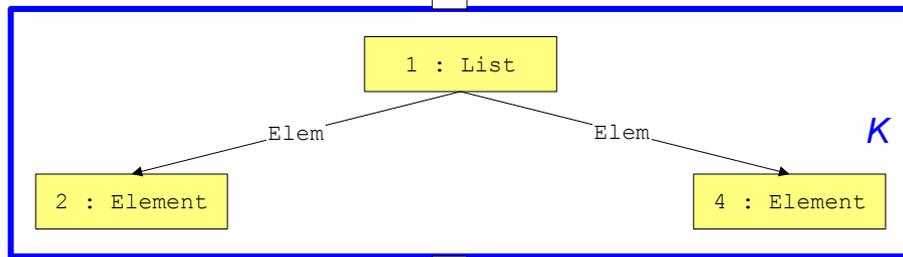
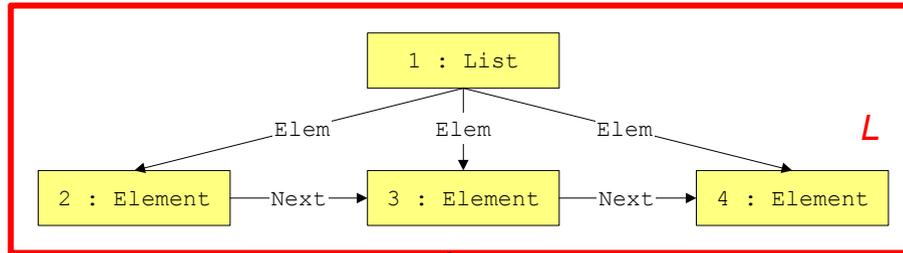
::=



end;

## Example of a graph rewrite rule (2)

`production DeleteElement =`



`end;`

## Application of a graph rewrite rule

### (Direct) derivation

A graph  $G'$  is derivable from a graph  $G$  by a rule  $r = (L, K, R) \Leftrightarrow$

- » There is an isomorphism  $h : L \rightarrow G_L$ , where  $G_L$  is a partial graph of  $G$  which determines the location of application of  $r$ .
- » Nodes and edges of  $G_L$  not appearing as images of  $K$  are deleted:

$$H = G \setminus (h(L) \setminus h(K))$$

- » Nodes and edges of  $R$  which do not belong to  $K$  are inserted:

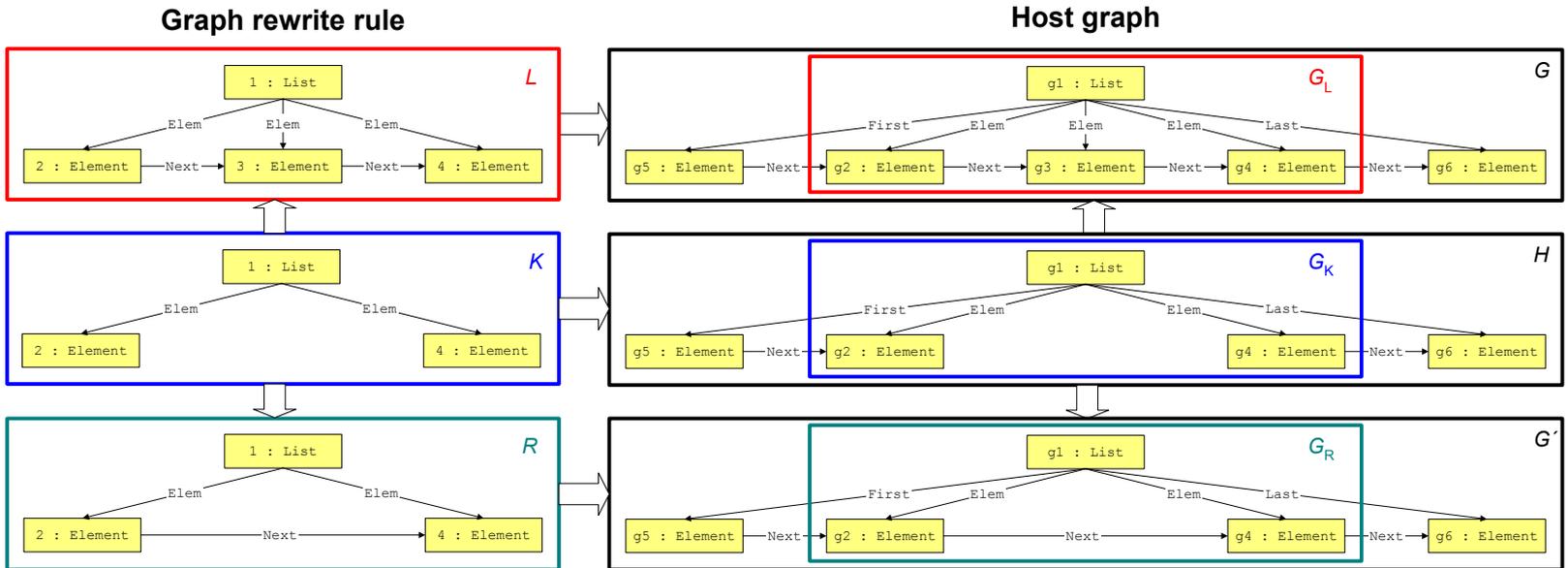
$$G' = H \oplus h'(R \setminus K), \text{ where}$$

- $\Rightarrow h'$  maps nodes of  $R \setminus K$  such that they do not occur in  $H$ ,
- $\Rightarrow$  Context edges with sources or targets from  $K$  are transferred to the respective nodes in  $h(K)$ .

## Other variants of graph rewrite rules

- $h$  need only be a morphism  $\Rightarrow$ 
  - » Higher flexibility by identification of graph elements
  - » Danger of undesired effects of rule applications
- $G_L$  must even be a subgraph  $G \Rightarrow$ 
  - » Larger left-hand sides
  - » Larger rule sets
- No edges from deleted nodes to context nodes  
(Dangling Edge Condition)  $\Rightarrow$ 
  - » Exclusion of undesired side effects
  - » Large left-hand sides
- Empty gluing graph  $\Rightarrow$ 
  - » Embedding of nodes of the right-hand side must be specified explicitly by embedding rules

# Example of the application of a graph rewrite rule



## Graph rewriting systems

### Definition: Graph rewriting system

A graph rewriting system is a tuple

$gs = (L_V, L_E, R, S)$  with:

- »  $L_V$  : finite set of node labels
- »  $L_E$  : finite set of edge labels
- »  $R$  : finite set of rules  $r = (L, K, R)$  ( $L, K, R$  graphs over  $L_V, L_E$ )
- »  $S$  : start graph (over  $L_V$  and  $L_E$ )

### Definition: Derivability

Let  $gs = (L_V, L_E, R, S)$  be a graph rewriting system. A graph  $G$  is derivable from the start graph  $S$  using the rule set  $R$   $gs \Leftrightarrow$

There is a sequence  $G_1 \dots G_n$  with

$S \rightarrow G_1 \dots \rightarrow G_n = G$

## Proof techniques

### Proof by induction

A predicate  $p$  is proved for all derivable graphs as follows ( $n$  : length of derivation):

- 1  $n = 0$ :  $p$  holds for the start graph  $S$ .
- 2  $n \rightarrow n + 1$ : Let  $G$  be a graph which may be derived in  $n$  steps from the start graph.

Induction assumption:  $p$  holds for  $G$ .

Induction conclusion:  $p$  holds for all graphs  $G'$  which may be derived from  $G$  by some rule  $r$  (in one derivation step).

(Induction conclusion has to be proved for all rules  $r$  and all potential locations of application.)

## Examples of (provable) properties of list graphs

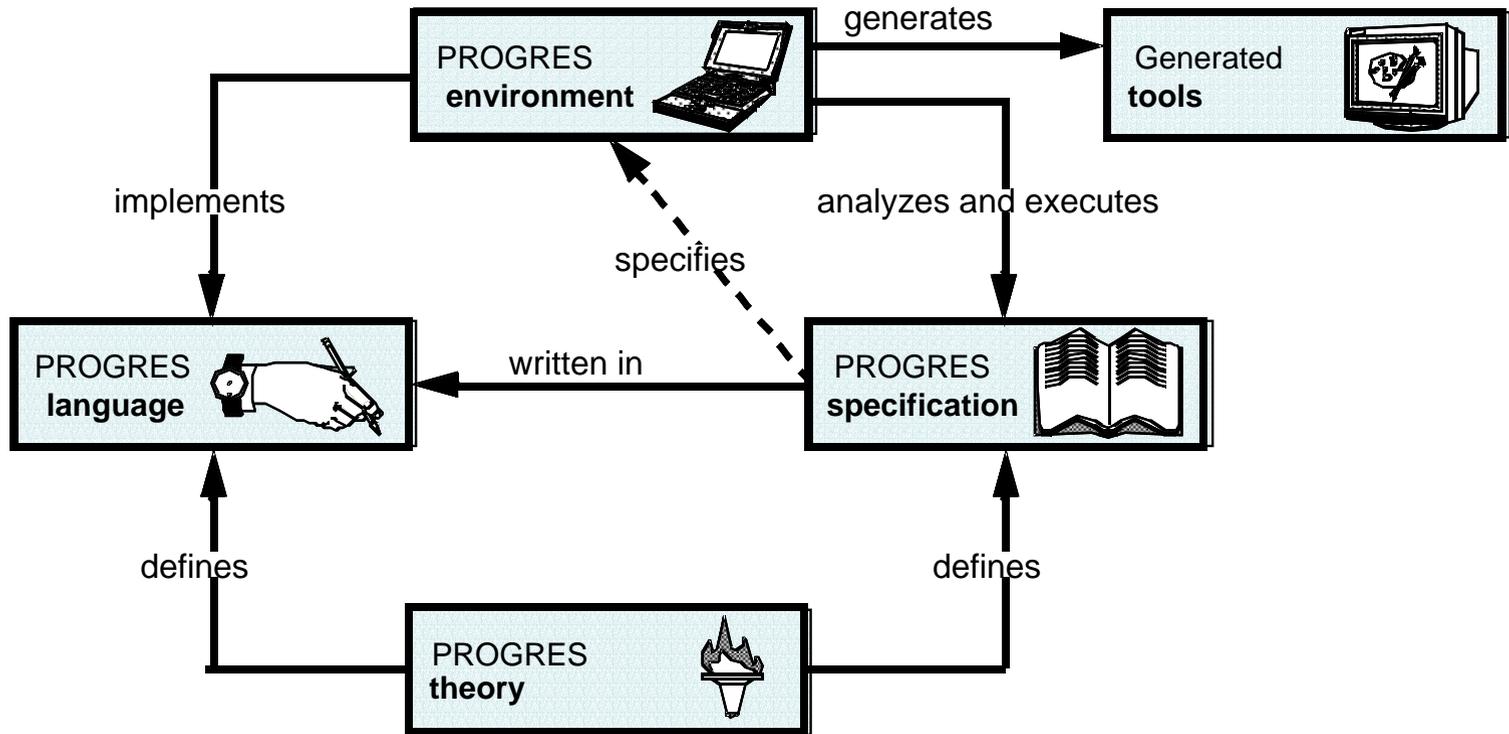
- ❑ Each list has at most one `First` element.
- ❑ Each list has at most one `Last` element.
- ❑ The `First` element does not have a predecessor.
- ❑ The `Last` element does not have a successor.
- ❑ Each element has at most one predecessor.
- ❑ Each element has at most one successor.
- ❑ ...

## Specification with PROGRES

## What is PROGRES?

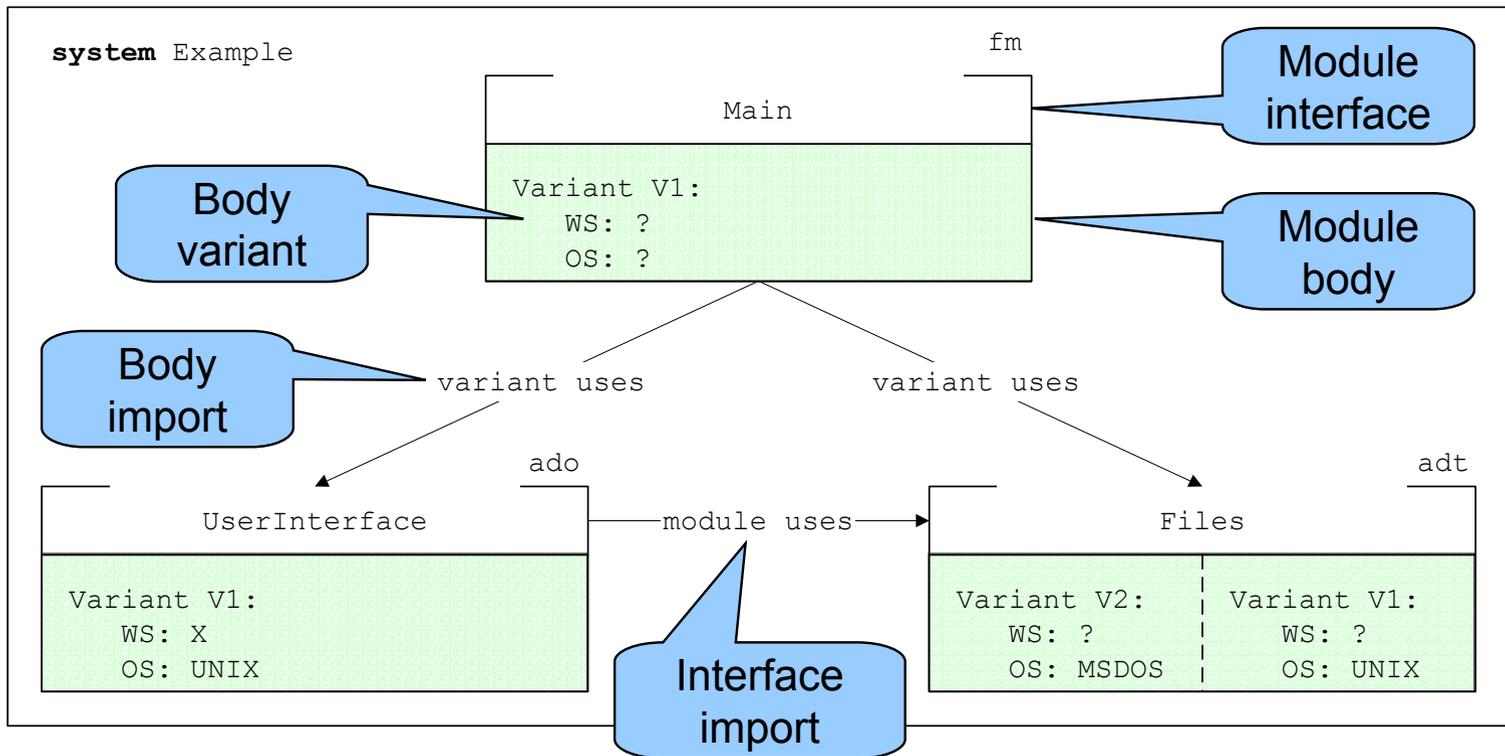
- ❑ **PROGRES = PRO**grammed **GR**aph **RE**writing **S**ystems
- ❑ Multiparadigmatic **Specification language**, based on graph rewriting
  - » Object-oriented modeling of graph schemata
  - » Declarative definition and incremental evaluation of derived attributes
  - » Rule-based and visual specification of graph tests and graph transformations
  - » Imperative and non-deterministic programming
- ❑ **Development environment** for the construction of specifications
  - » Syntax-aided editor
  - » Static analyses
  - » Interpreter
  - » Code generator

# Components of PROGRES



# Example

## Tools for programming-in-the-large



## Explanations

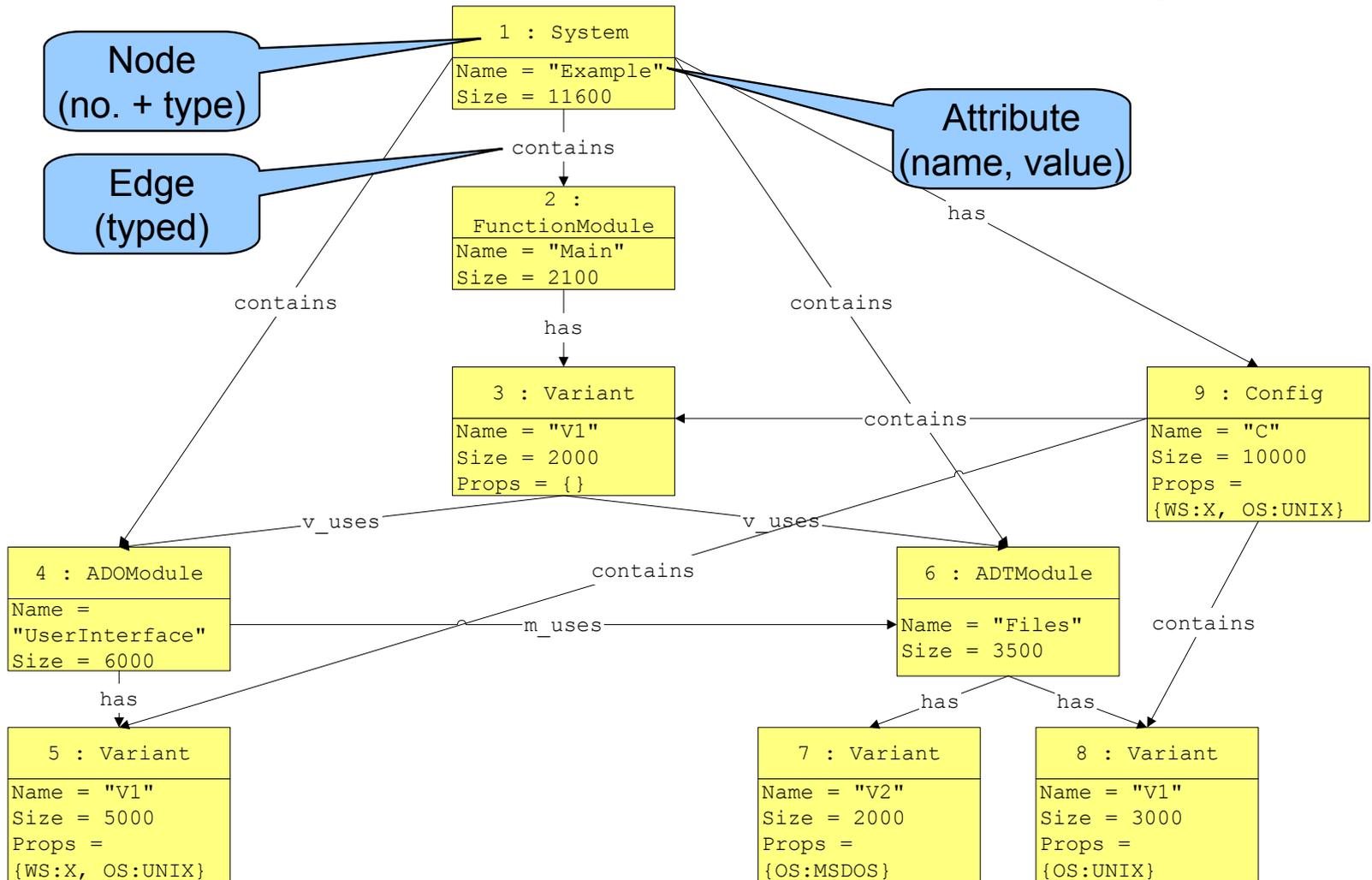
- ❑ There are three types of modules (fm, ado, adt).
- ❑ The function module (fm) `Main` exports a set of functions; it has exactly one body variant.
- ❑ This variant imports the modules `UserInterface` and `Files`.
- ❑ The data object module (ado) `UserInterface` realizes a data store and its access operations (in exactly one variant).
- ❑ The interface of module `UserInterface` imports from the module `Files` the type `File`.
- ❑ The data type module (adt) `Files` exports a data type with operations for creating and manipulating an arbitrary number of instances; it has two variants.
- ❑ Properties of variants are defined through a set of attributes (`WS` for Window System and `OS` for Operating System).
- ❑ Attributes either have concrete values (like `UNIX` or `MSDOS`) or are undefined.

## Desired tool functionality

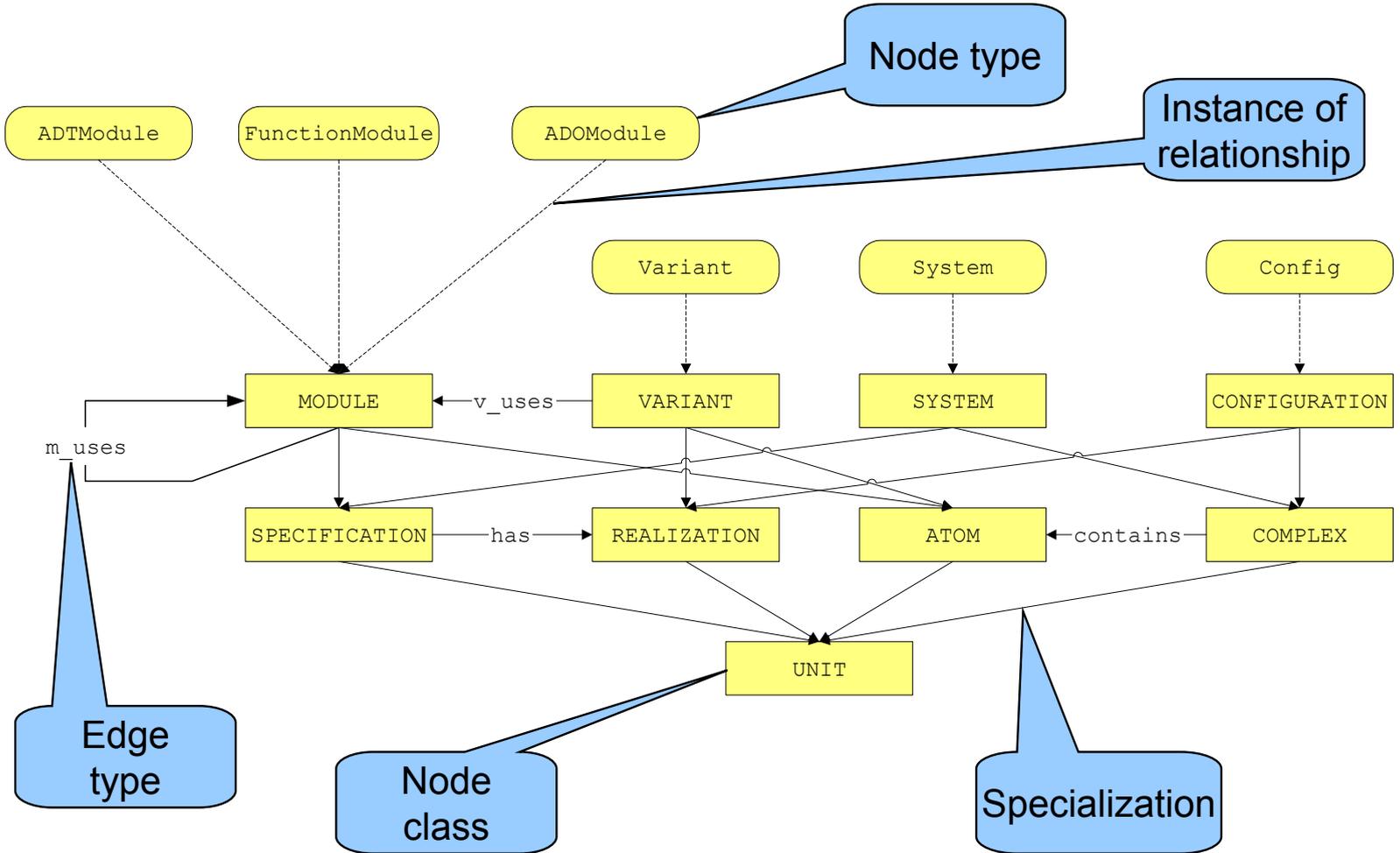
- ❑ Syntax-aided editing of module graphs (context free correctness is enforced, e.g. variant import do not emanate from module interfaces)
- ❑ Checking of context sensitive constraints (e.g., no import cycles)
- ❑ Completely automatic or semi-automatic configuration of system variants satisfying given properties  
(Attention: Requires consistent selection of variants. In the example, there is only one consistent configuration for  $WS = X$  and  $OS = UNIX$ .)

## Attributed Graphs and Graph Schemata

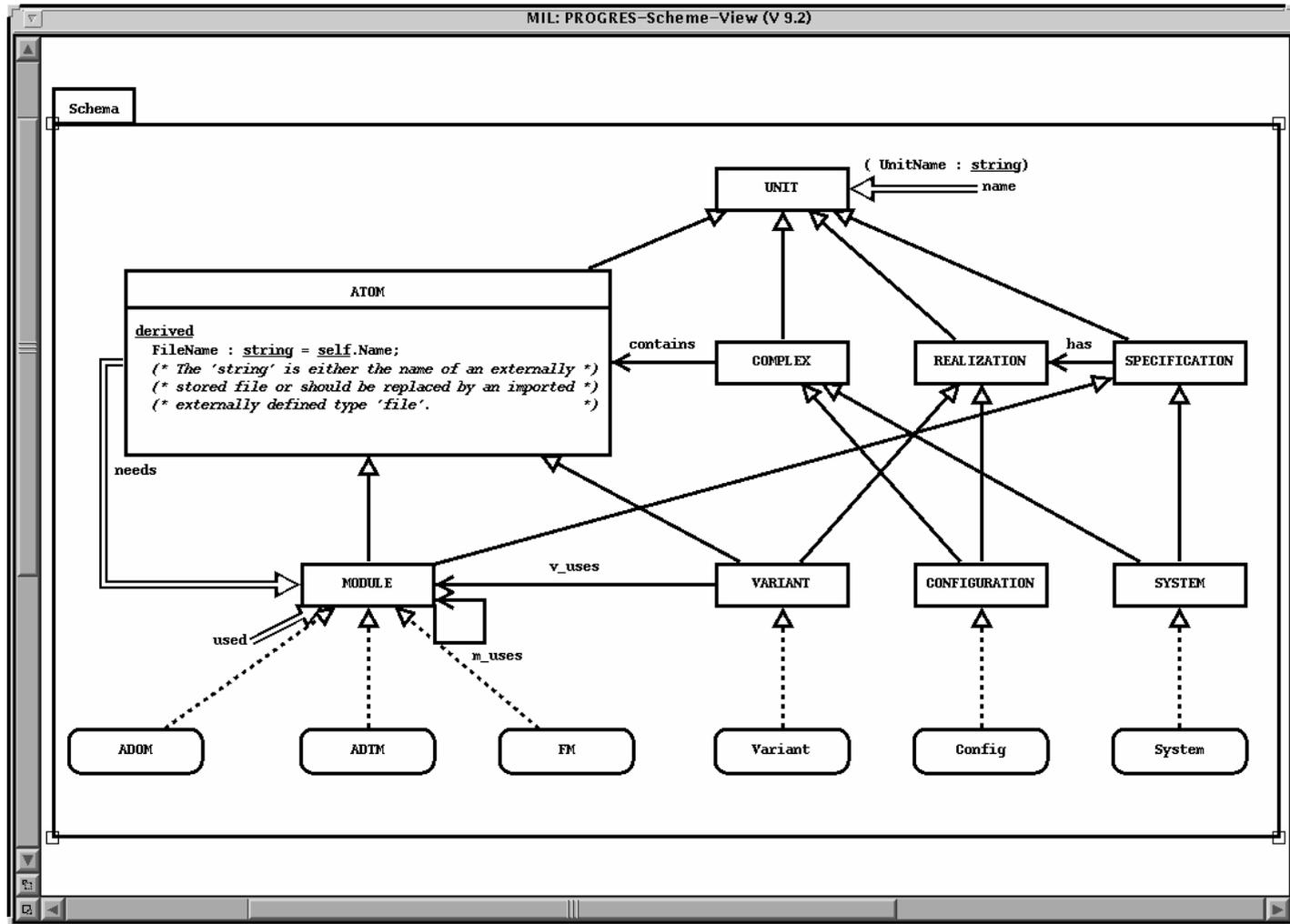
# Representation of the example as an attributed graph



# Graphical definition of a graph schema



# PROGRES schema editor



## Definition of attributes

- ❑ A graph schema may be specified both textually and graphically.
- ❑ Attributes and attribute evaluation rules may be defined in a textual (sub-)view.
- ❑ Intrinsic attributes receive their values by explicit assignment and may be initialized with a constant.
- ❑ Derived attributes are calculated from the attribute values of related nodes with the help of a (directed) equation.
- ❑ Related nodes are all nodes which may be reached via a path, e.g.:
  - » `self` : Returns the current node
  - » `-e->` and `<-e-`, respectively : Traversal of edges of type `e` (in forward and backward direction, respectively)
  - » Concatenation : `p1 & p2`

## Textual definition of a graph schema (1)

```

node class UNIT
  derived
    Size : integer = 0;
  intrinsic
    Name : string := "";
end;  (* Root of class hierarchy. *)

node class SPECIFICATION is a UNIT
  redef derived
    Size = max( 0, all self.-has->.Size );
    (* The 'Size' of a specification is the maximum of *)
    (* the size of all its realizations, instead of *)
    (* being the sum (which would reasonable, too). *)
end;  (* A 'SPECIFICATION' is either the complete design of *)
      (* a software system or a design of one its parts. *)

node class REALIZATION is a UNIT
  intrinsic
    Props : string [0:n];  (* Set of guaranteed properties *)
end;  (* A 'REALIZATION' is an implementation of a 'SPEC.' *)
      (* which fulfills a given set of properties like *)
      (* needed hardware platforms, operating system *)

```

## Textual definition of a graph schema (2)

```

edge type has : SPECIFICATION [1:1] -> REALIZATION [0:n];
    (* A 'SPECIFICATION' 'has' an arbitrary number of      *)
    (* 'REALIZATIONS', but a 'REALIZATION' belongs to a    *)
    (* uniquely defined 'SPECIFICATION'.                    *)

```

```

node class COMPLEX is a UNIT
    redef derived
        Size = addSize( 0, all self.-contains-> );
        (* The 'Size' of a complex unit is the sum of *)
        (* the 'Size' of all its children.            *)
    end;

```

```

node class ATOM is a UNIT
    intrinsic
        File : file;      (* Pointer to externally stored file. *)
    redef derived
        Size = size( self.File );
        (* 'Size' is the length of the attached File *)
    end;

```

```

edge type contains : COMPLEX [1:1] -> ATOM [0:n];
    (* A 'COMPLEX' may contain 0 to n 'ATOM' nodes. *)
    (* Conversely, an 'ATOM' node is contained in exactly *)
    (* one 'COMPLEX'. *)

```

Edge type

Cardinality

## Textual definition of a graph schema (3)

```

node class SYSTEM is a SPECIFICATION, COMPLEX
  redef derived
    Size = addSize( 0, all self.-contains-> );
      (* Resolves inheritance conflict of attribute *)
      (* definitions in 'SPECIFICATION' and 'COMPLEX' *)
      (* by preferring definition in 'SPECIFICATION'. *)
  end;

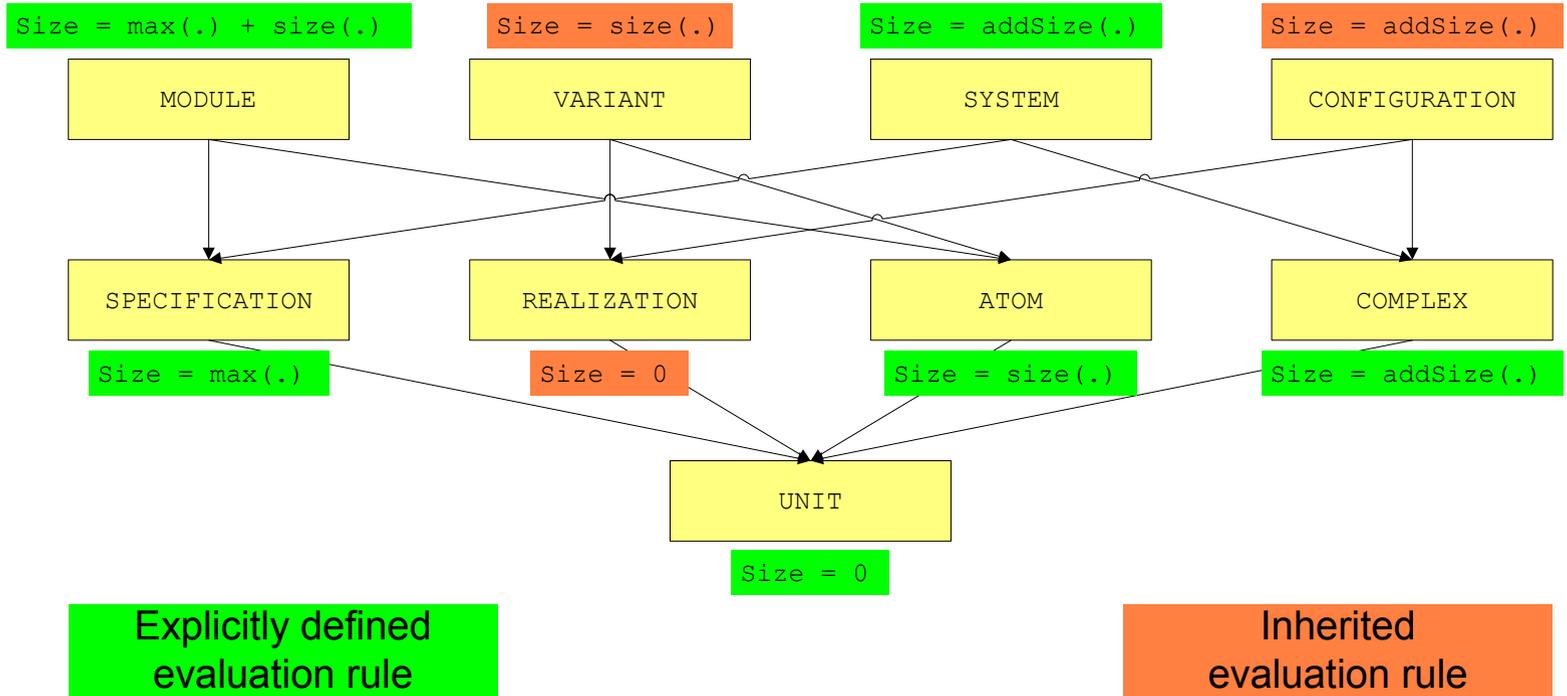
node class CONFIGURATION is a REALIZATION, COMPLEX end;
  (* A 'CONFIGURATION' is a set of variants of module *)
  (* realizations which fulfill all required properties. *)

node class MODULE is a SPECIFICATION, ATOM
  redef derived
    Size = size( self.File ) + max( 0, all self.-has->.Size );
      (* Resolves inheritance conflict of attribute *)
      (* definitions in 'SPECIFICATION' and 'COMPLEX' *)
      (* by building the sum of both definitions which *)
      (* are in conflict to each other. *)
  end;
  (* A 'SYSTEM' contains a set of 'MODULES' which *)
  (* have 'VARIANTS' as their realizations. *)

node class VARIANT is a REALIZATION, ATOM end;

```

## Attribute redefinition conflicts



## Path expressions and restrictions

- A **path expression** is
  - » a derived relation between nodes (edges are intrinsic relations):  
 $v_1 =_p \Rightarrow v_2 \Leftrightarrow$  There is a path  $p$  from  $v_1$  to  $v_2$
  - » a function on node sets:  
 $p(V) = \{ v_2 \mid \exists v_1 \in V : v_1 =_p \Rightarrow v_2 \}$
- A **restriction** is a “unary path expression”, i.e., a set of nodes is restricted to those elements which satisfy a certain condition.
- Path expressions and restrictions may be specified:
  - » textually
  - » graphically

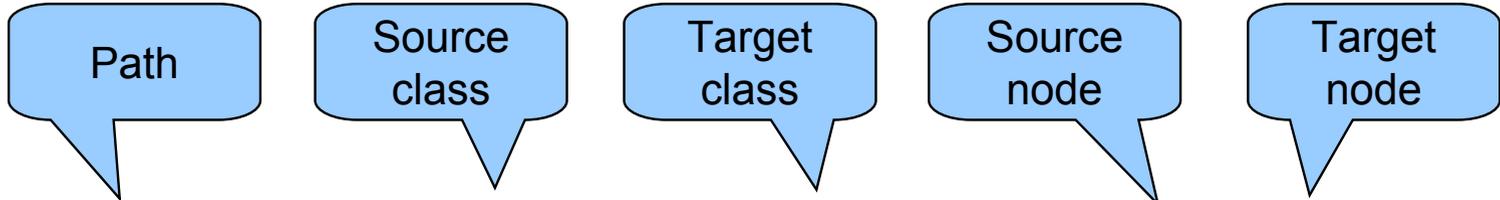
## Textual path expressions

Operator	Semantics
$p \& q$	Concatenation of $p$ and $q$
$p \text{ or } q$	Connection by $p$ or $q$
$p \text{ and } q$	Connection by $p$ and $q$
$p \text{ but not } q$	Connection by $p$ but not by $q$
$[p \mid q]$	Connection by $p$ , else by $q$
$p^+$	Transitive closure
$p^*$	Reflexive and transitive closure
$\{p\}$	Maximal iteration

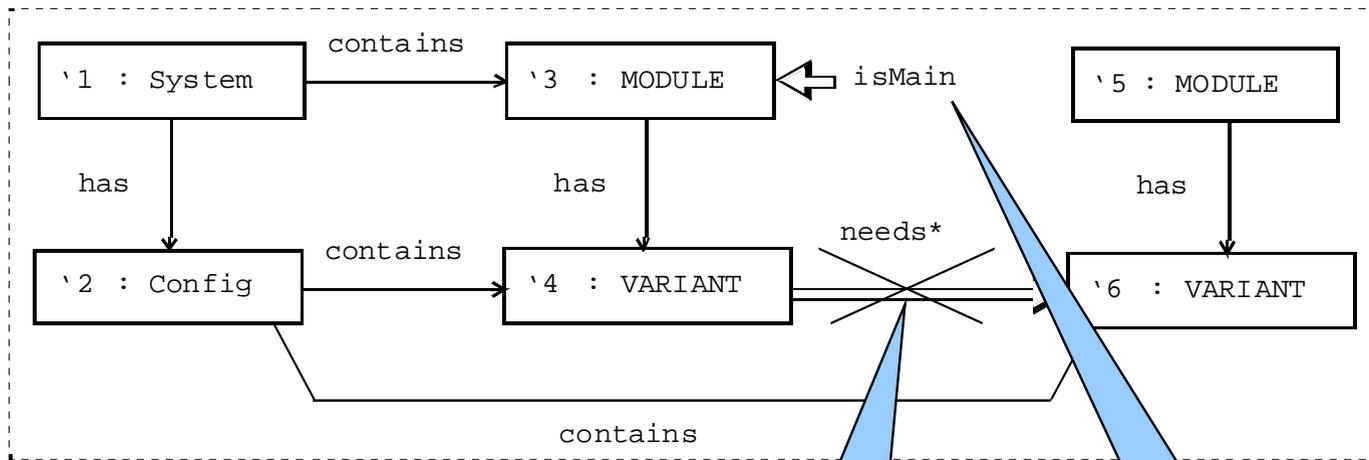
## Examples of textual path expressions

```
path needs : ATOM [0:n] -> MODULE [0:n] =  
    (* The path 'needs' connects any variant or module to its imports. *)  
    ( instance of MODULE & =moduleNeeds=> )  
    or ( instance of VARIANT & =variantNeeds=> )  
end;  
  
path moduleNeeds : MODULE [0:n] -> MODULE [0:n] = -m_uses-> end;  
  
path variantNeeds : VARIANT [0:n] -> MODULE [0:n] =  
    -v_uses-> or ( <-has- & instance of MODULE & -m_uses-> )  
end;  
  
path dependsOn : MODULE [0:n] -> MODULE [0:n] =  
    (* connects module to its interface imports & imports of its variants. *)  
    ( self or -has-> ) & =needs=>+  
end;
```

## Example of a graphical path expression



path UselessVariant : Config [0:n] -> VARIANT [0:n] = from '2 to '6 in



end;

(\* searches for all variants which are contained in a configuration but are not reachable from the top-level module \*)

(Negative) path

Restriction

# Graph Rewrite Rules

## Composition of graph rewrite rules

production P ( parameter list ) =

Left-hand side with:

- single nodes, set nodes, negative/optional nodes
- positive and negative edges between pairs of nodes
- positive and negative paths between pairs of nodes
- node restrictions

::=

Right-hand side with:

- single nodes, set nodes, optional nodes
- edges between pairs of nodes

fold Specified nodes may be identified;

condition Conditions on attributes of left-hand side nodes;

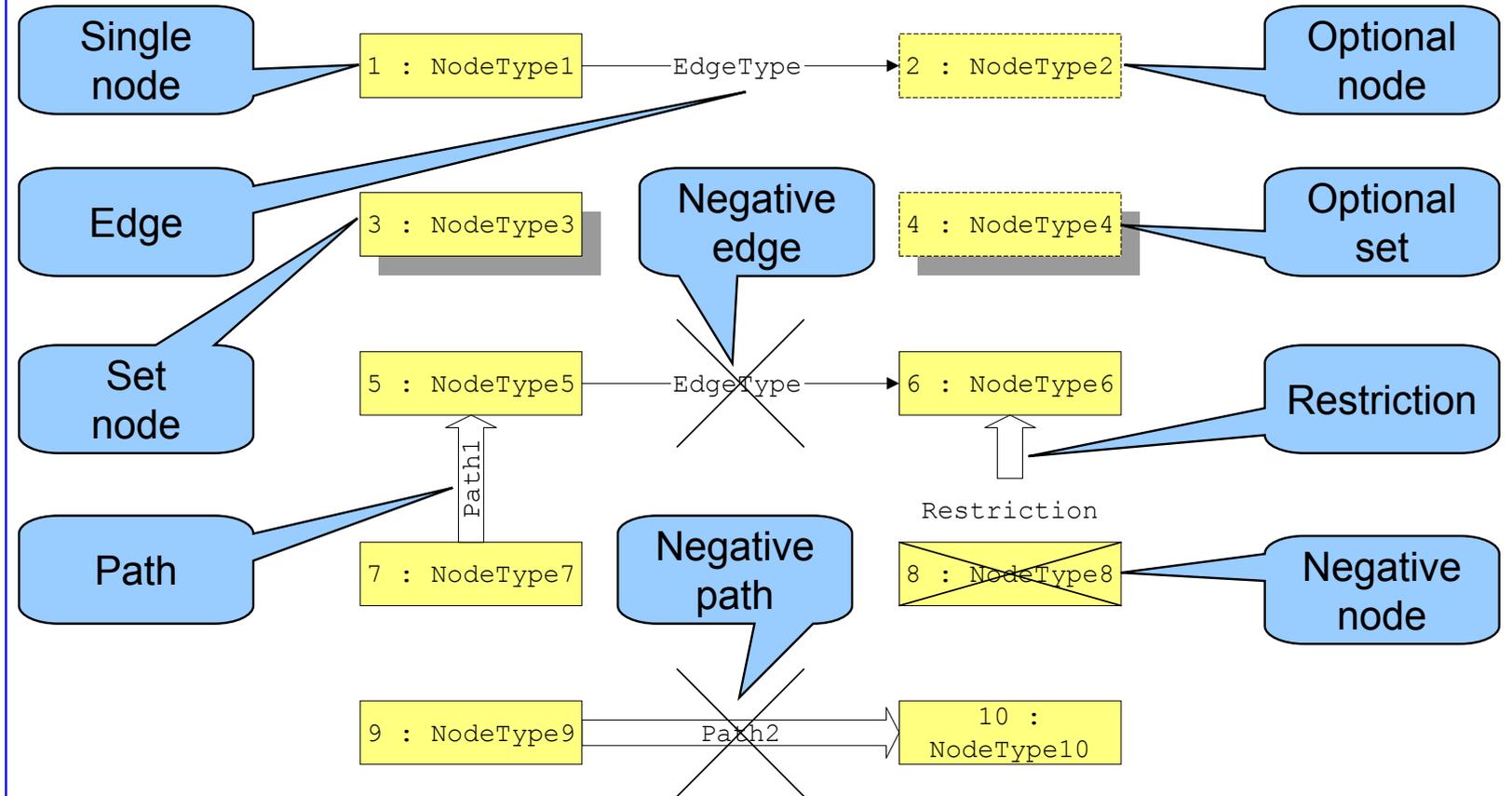
embedding Embedding rules for nodes of right-hand side;

transfer Attribute assignments for nodes of right-hand side;

return Assignments to out parameters;

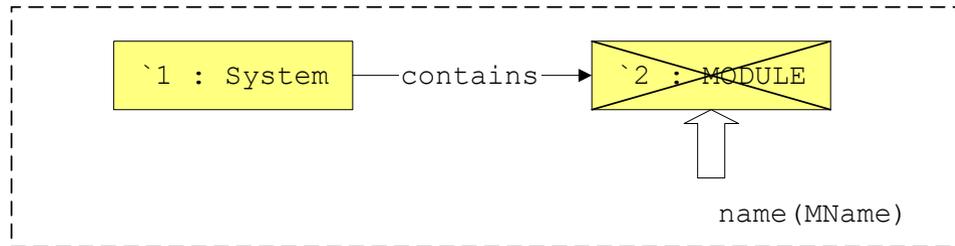
end;

## Elements of left-hand sides and right-hand sides



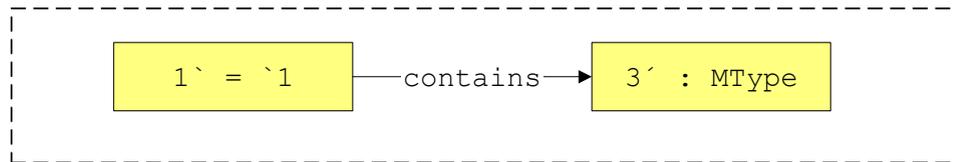
## Example for parameters, negative nodes, attribute transfer, etc.

```
production CreateModule (MName : string; InterfaceDescription : file;
                        MType : type in MODULE; out NewM : MODULE) =
```



(\* Creates a module with name 'MName' if the 'System' does not already contain a module with this name. The 'Mtype' parameter is a 'FunctionModule' or 'ADTModule' or 'ADOModule'. \*)

::=

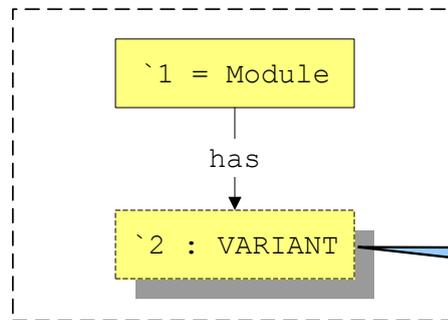


```
condition \2.Name = MName; (* Conditions only for normal nodes *)
transfer 3'.Name := MName;
          3'.File := InterfaceDescription; (* External file handle. *)
return   NewM := 3';
end;
```

```
restriction name (UName : string) : UNIT = valid (self.Name = UName) end;
(* The restriction is valid if the current 'UNIT' is named 'UName'. *)
```

## Example of optional set nodes

production DeleteModule (Module : MODULE) =



Optional set

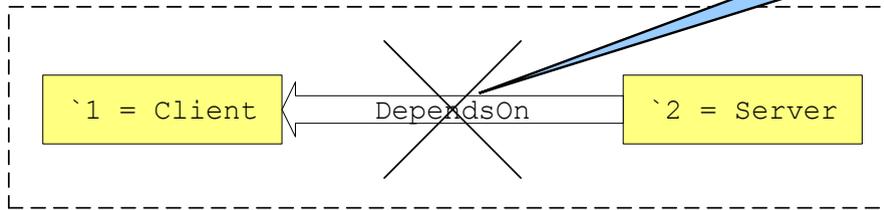
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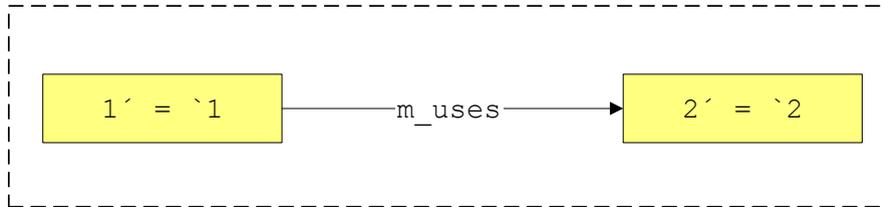
end;

## Example of a negative path

```
production CreateMUse(Client, Server : MODULE) =
```



```
::=
```



```
end;
```

Negative path

*(\* Creates a new import from 'Client' to 'Server'. \*)*

## Embedding rules

Rule	Semantics
<u>copy</u> $-e-\>$ <u>from</u> $\`n$ <u>to</u> $m'$	Copy outgoing $e$ edges from node $\`n$ of the left-hand side to node $m'$ of the right-hand side
<u>remove</u> $-e-\>$ <u>from</u> $\`n$	Delete outgoing $e$ edges from node $\`n$
<u>redirect</u> $-e-\>$ <u>from</u> $\`n$ <u>to</u> $m'$	Redirect outgoing $e$ edges from $\`n$ to $m'$
$\langle -e -$ instead of $-e -\rangle$	Analogously for incoming rather than outgoing edges
$-e -\rangle$ <u>as</u> $-f -\rangle$ instead of $-e -\rangle$	Relabeling
$-e -\rangle$ <u>as</u> $\langle -f -$ statt $-e -\rangle$	... and change of direction

## Example of embedding rules

```
production ChangeModuleType (Module : MODULE; NewType : type in MODULE;
                               out NewNode : NewType) =
```

```
`1 = Module
```

```
::=
```

```
1' : NewType
```

*(\* Replaces given module by a module of type 'NewType' with same edges and attribute values. Unfortunately, this has to be handled by deletion and re-insertion. \*)*

```
embedding redirect -m_uses->, -has->, <-contains-,
                    <-m_uses-, <-v_uses- from `1 to 1';
```

```
transfer 1'.Name := `1.Name;
         1'.File := `1.File;
return NewNode := 1';
end;
```

Embedding rule

# PROGRES rule editor

MIL: PROGRES-View-1 (V 9.2)

```

production ResolveImport( C : CONFIGURATION ; ReqProps : string [0:n] ;
                        out NewProps : string [0:n] )
=

```

```

::=

```

```

condition '2.Props 'are_in' ReqProps;
return NewProps := merge ( ReqProps, 2'.Props );
end;
(* Selects a module which is used by a 'Variant' in *)

```

**Executable Commands**

- EDIT
- ANALYZE
- BROWSE
- CONSTRAINT
- DISPLAY
- INTERPRET
- LAYOUT
- MISC
- UN/REDO
- VERSION
- HELP
- QUIT

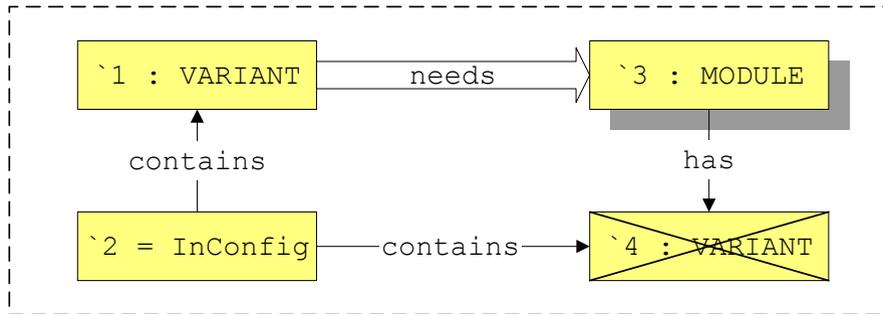
Generic

- ChangeCard
- RestrictCond (Er)
- NotPathCond (E~)
- NotEdgeDecl (En)
- PathCond (Ep)
- EdgeDecl (Ee)
- NotNodeDecl (E-)
- OptSetDecl (E\*)
- OblSetDecl (E+)
- OptNodeDecl (EO)
- OblNodeDecl (E1)

Cmd (abbr):

## Example of a graph test

```
test UnresolvedImport(InConfig : Config; out MSet : MODULE [1:n]) =
```



```
return MSet := `3;
```

```
end;
```

*(\* Returns all modules which are needed by some variant already selected but for which no variant is included yet in the configuration. \*)*

## Searching for subgraphs

- ❑ Complexity of naive implementation:  $o(n^k)$   
(for each of  $k$  nodes in  $L$  there are  $n$  candidates in  $G$ ).
- ❑ Heuristics (sketch):
  - » Start at those nodes which are fixed by input parameters.
  - » Extend the match by nodes which may be determined in a unique way (incoming or outgoing edges of cardinality 1).
  - » Process remaining candidate sets by increasing cardinality.
  - » Process set nodes at the end.

## Control Structures

## Control structures: motivation and properties

- ❑ Composition of graph tests into complex **queries**  
(which do not modify the host graph)
- ❑ Composition of graph rewrite rules (and graph tests) into complex **transactions**
- ❑ **ACID** properties of transactions (and graph rewrite rules):
  - » **Atomic**: either complete execution or no modification of the host graph
  - » **Consistent**: consistency-preserving transformation
  - » **Isolated**: isolation in multi-user mode
  - » **Durable**: persistent
- ❑ Additional property: **non-determinism**
- ❑ Failure of executing an operation results in **backtracking**

## Overview of control structures

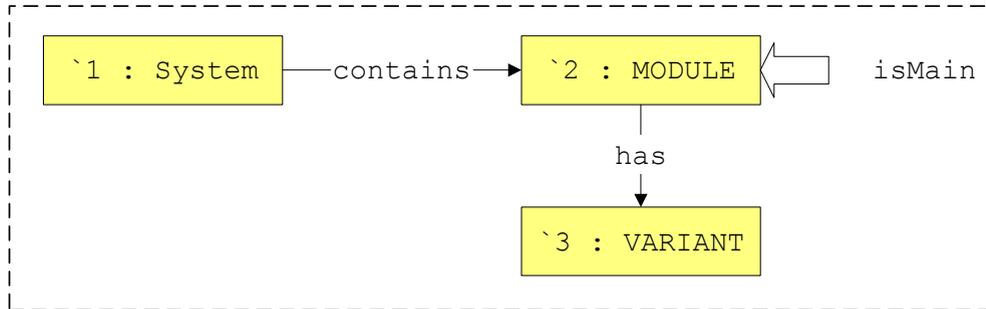
Control structure	Semantics
<code>p &amp; q</code>	Sequence
<code>p <u>and</u> q</code>	<code>p</code> und <code>q</code> in any order
<code>p <u>or</u> q</code>	Non-deterministic choice
<code><u>choose</u> p1 <u>else</u> p2 ... <u>end</u></code>	Try <code>p1</code> , else <code>p2</code> ...
<code><u>loop</u> p <u>end</u></code>	Loop (execute <code>p</code> as long as possible)
<code><u>for</u> <u>all</u> n <u>do</u> p <u>end</u></code>	Execute <code>p</code> for all nodes <code>n</code>
<code><u>use</u> v : ... <u>do</u> p <u>end</u></code>	Block with declaration of variables

## Example of a transaction with backtracking

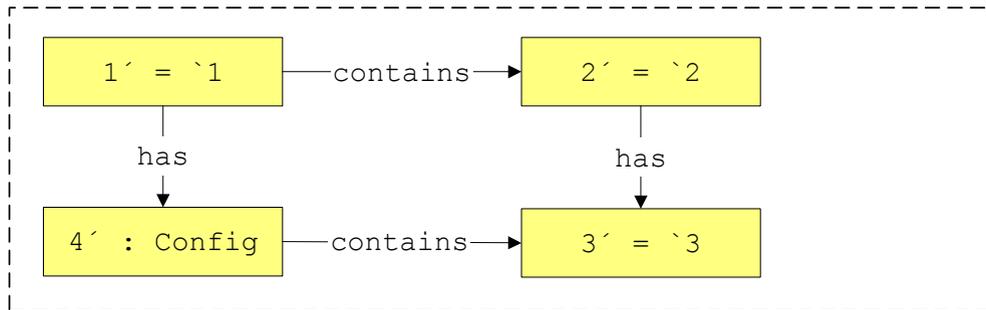
```
transaction CreateConfig(CName : string; CProps : string [0:n]) =  
  use ReqProps := CProps do  
    InitConfig(CName, ReqProps, out ReqProps)  
  & loop  
    ResolveImport(CName, ReqProps, out ReqProps) (* see p. 56 *)  
  end  
  & not UnresolvedImportExists(CName) (* similarly to p. 57 *)  
end  
end;
```

## Rule for initializing a configuration

```
production InitConfig(CName : string; CPropsIn : string; out CPropsOut : string) =
```



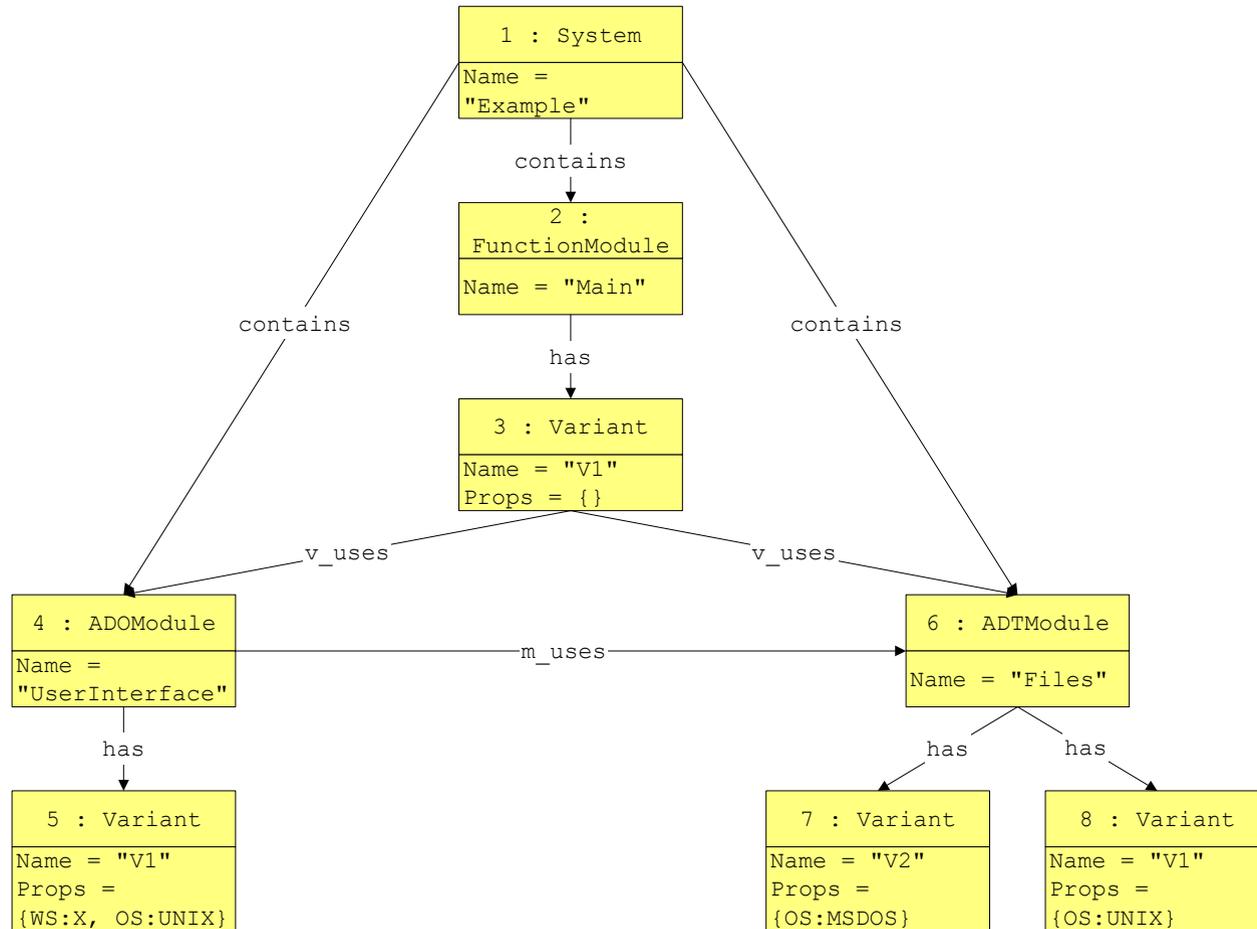
```
::=
```



```

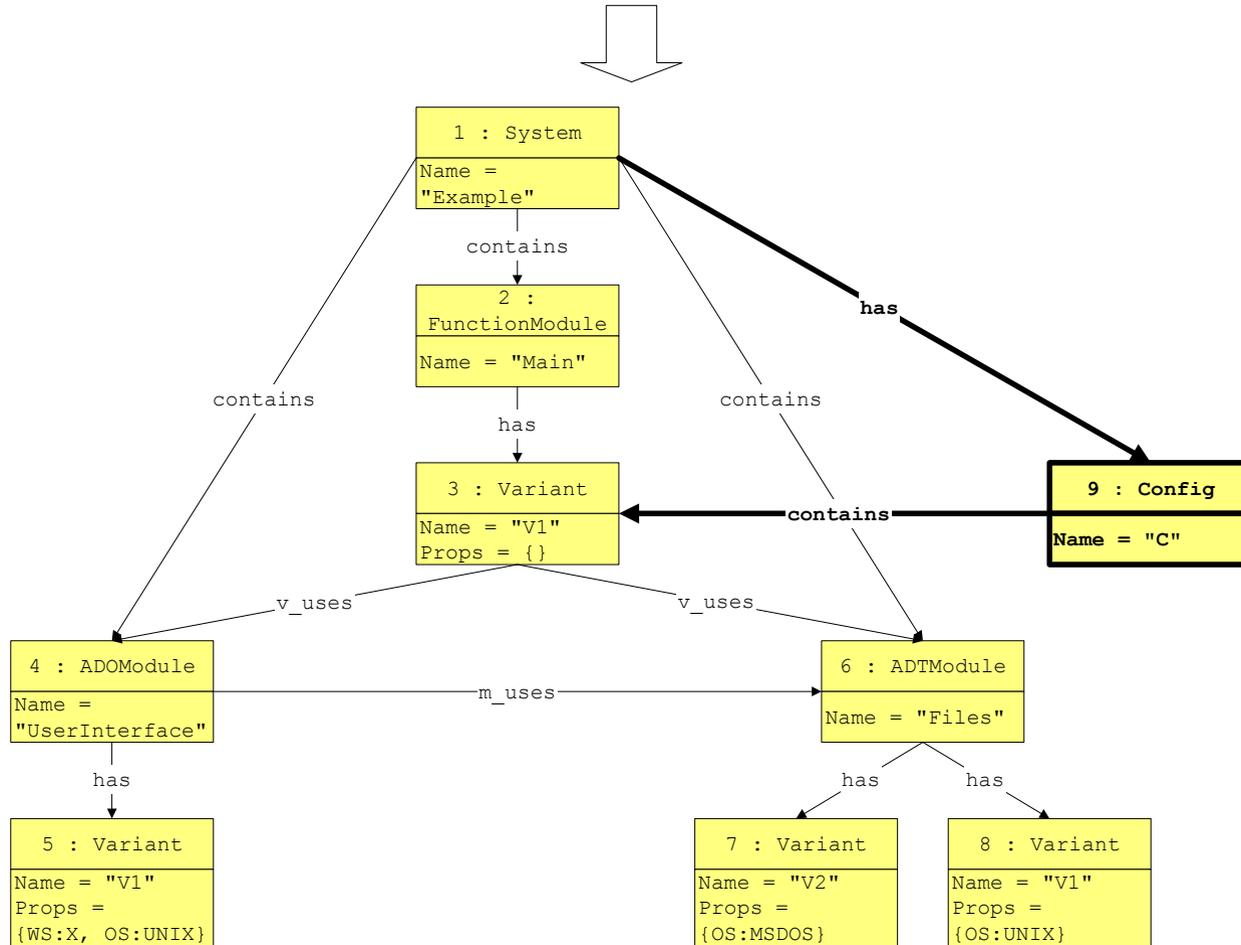
condition `3.Props in CPropsIn;
transfer 4'.Name := CName;
return CPropsOut := merge(`3.Props, CPropsIn);
end;
  
```

## Example (1)



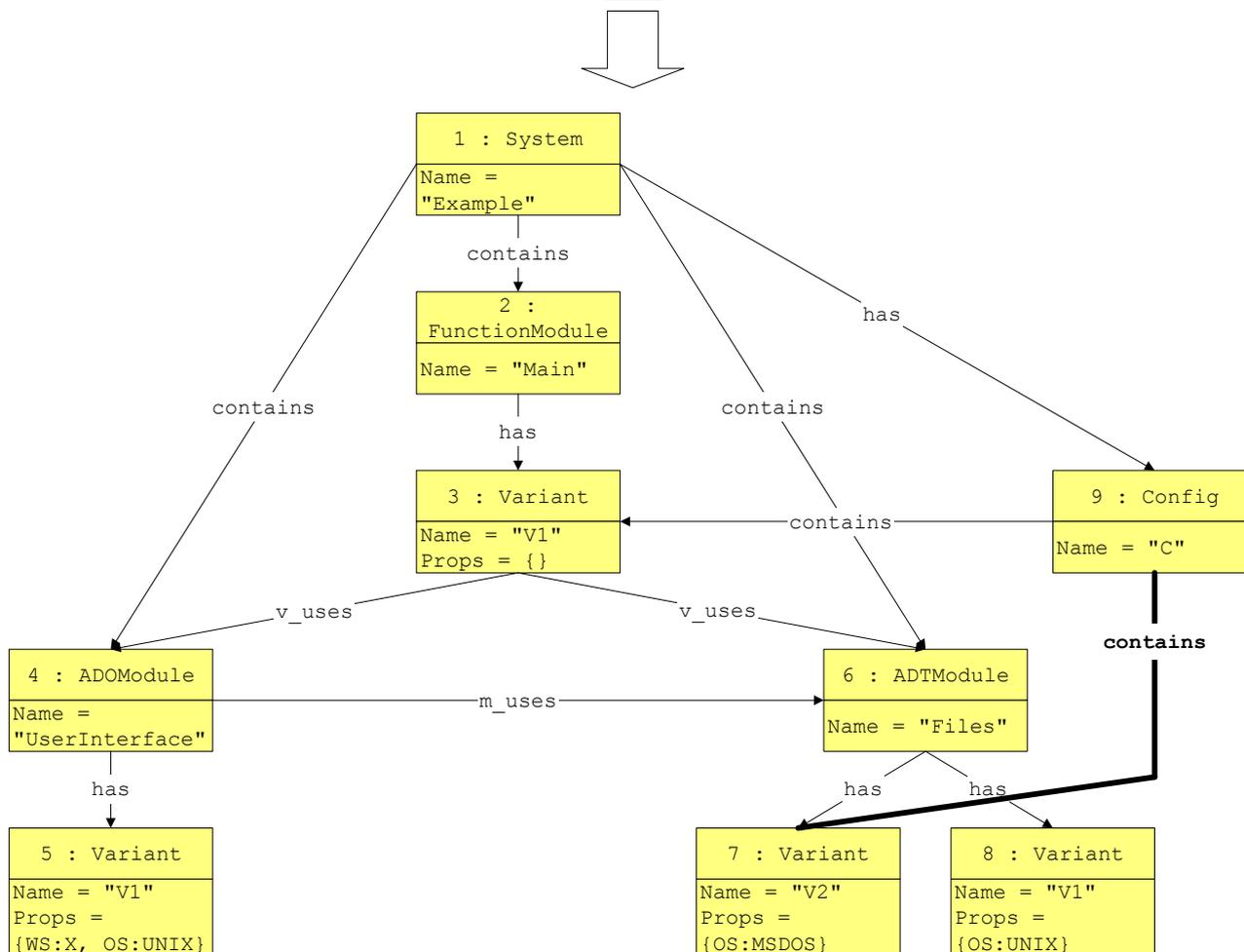
## Example (2)

InitConfig("C", {}, out ReqProps = {})



## Example (3)

`ResolveImport("C", {}, out ReqProps = {OS:MSDOS})`

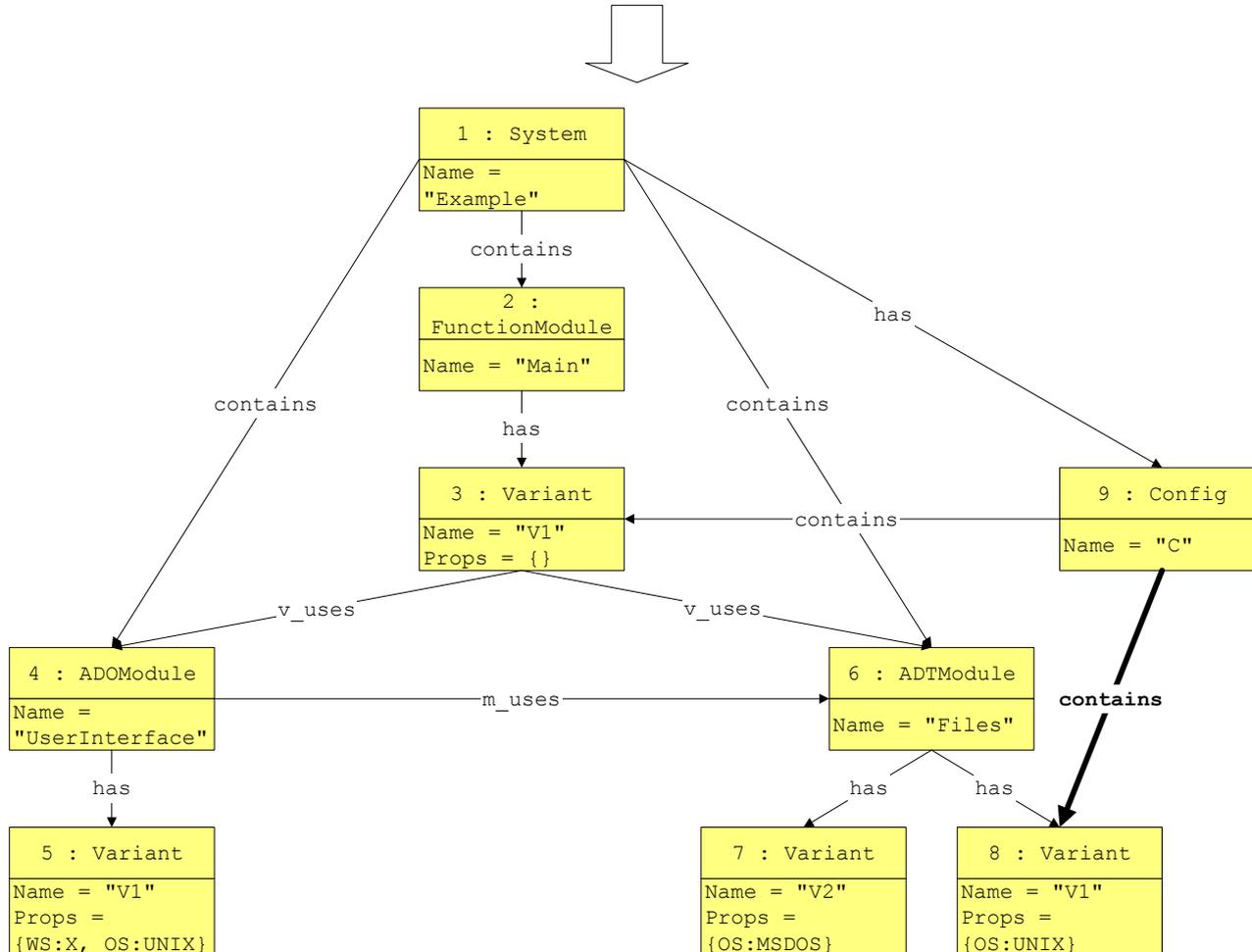


## Example (4)

- ❑ `ResolveImport` fails for the module `UserInterface` because `{OS:UNIX} in {OS:MSDOS}` does not hold.
- ❑ Loop terminates successfully, but the subsequent test `UnresolvedImportExists` reveals an unresolved import.
- ❑ As a result of backtracking, the previous selection of the variant of `Files` is revised (slide 68 shows the situation after selection of another variant).
- ❑ Finally, a variant of `UserInterface` may be selected successfully (slide 69).

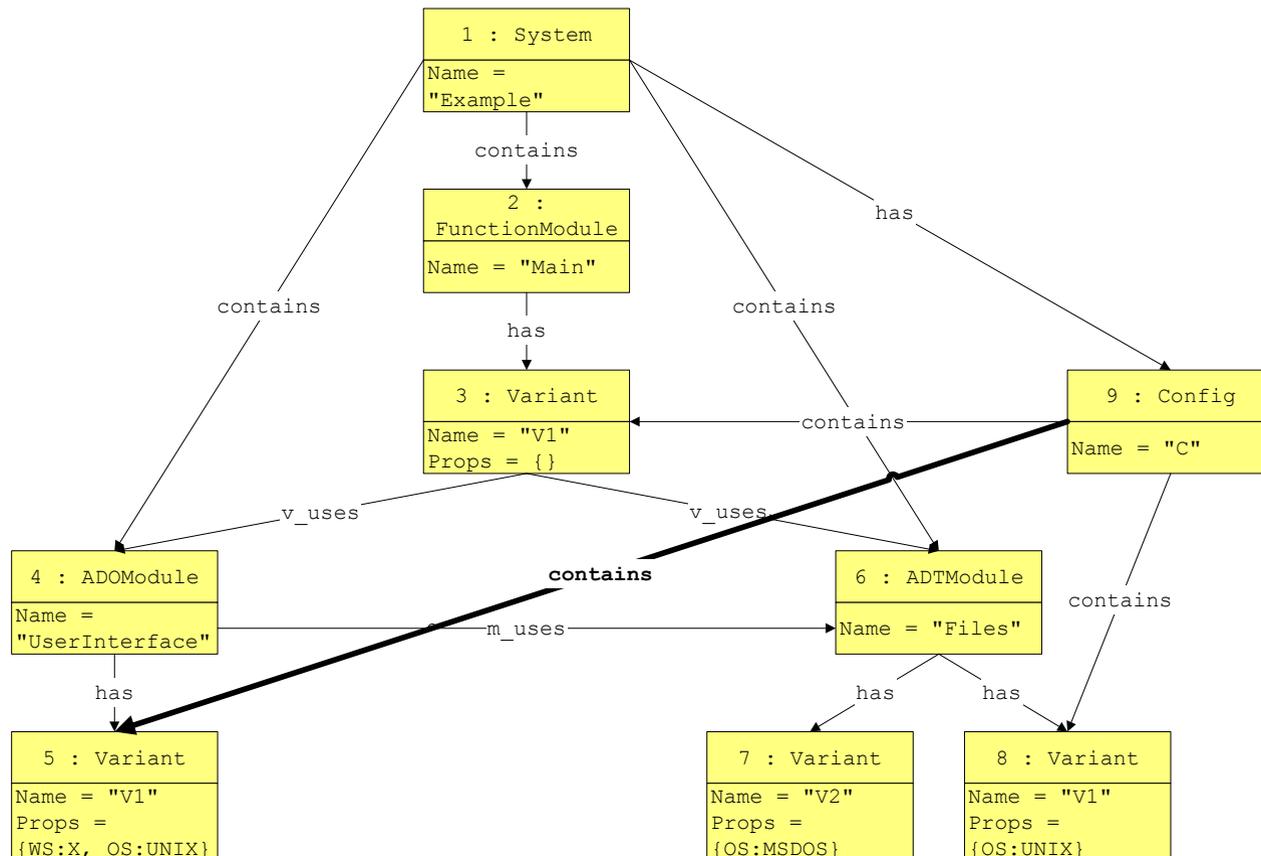
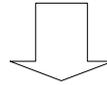
## Example (5)

`ResolveImport("C", {}, out ReqProps = {OS:UNIX})`



## Example (6)

ResolveImport("C", {OS:UNIX}, out ReqProps = {WS : X, OS:UNIX})



# Summary

## Advantages of specifying with graph rewrite rules

- ❑ Graphs are an appropriate data model for a large set of applications.
- ❑ Even complex data structures with a high number of consistency constraints may be represented as graphs.
- ❑ Complex graph transformations may be specified declaratively by graph rewrite rules.
- ❑ Visual programs composed of graph rewrite rules are easy to comprehend.
- ❑ The specification is operational, code generation is supported (for rapid prototyping).

## Disadvantages of specifying with graph rewrite rules

- ❑ Generality is constrained: commitment to a specific data model.
- ❑ For simple data types, graphs and graph transformations are an “overkill”.
- ❑ Potential efficiency problems (subgraph search is NP-complete).
- ❑ In case of PROGRES:
  - » Very expressive, but also very complex language.
  - » Specifying-in-the-large not completely elaborated.

## Literature

- ❑ G. Rozenberg (Ed.): **Handbook of Graph Grammars and Computing by Graph Transformation, Vol. 1: Foundations**, World Scientific (1997)  
*Collection of papers on the theory of graph rewriting systems*
- ❑ H. Ehrig et al. (Eds.): **Handbook of Graph Grammars and Computing by Graph Transformation, Vol. 2: Applications, Languages and Tools**, World Scientific (1999)  
*Applications of graph rewriting systems, including e.g. chapters on PROGRES and its applications*
- ❑ A. Schürr: **Operationales Spezifizieren mit programmierten Graphersetzungssystemen**, Deutscher Universitätsverlag, Wiesbaden (1991)  
*PROGRES language definition (in German)*
- ❑ A. Schürr, B. Westfechtel: **Graphgrammatiken und Graphersetzungssysteme**, script for the corresponding lecture, Aachener Informatik-Berichte 92-15 (1992)  
*Survey of the most important approaches concerned with graph rewriting*